

## SSLC EXAMINATION, MARCH - 2021

## MATHEMATICS

(English)

Time : 2½ Hours

Total Score : 80

## Instructions :

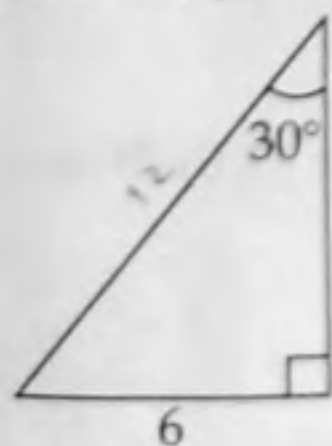
- 20 minutes is given as cool-off time.
- Use cool-off time to read the questions and plan your answers.
- Attempt the questions according to the instructions.
- Keep in mind, the score and time while answering the questions.
- The maximum score for questions from 1 to 45 will be 80.
- No need to simplify irrationals like  $\sqrt{2}$ ,  $\sqrt{3}$ ,  $\pi$  etc., using approximations unless you are asked to do so.

Score

For questions from 1 to 5, choose the correct answer from the brackets. Each question carries 1 score.

5x1=5

1. Arithmetic sequence with common difference 2 is : 1  
 [7, 10, 13, ... ; 7, 5, 3, ...]  
~~[7, 9, 11, ... ; 2, 5, 8, ...]~~
2. Which is always a cyclic quadrilateral ? 1  
 [Parallelogram ; Square]  
~~[Trapezium ; Rhombus]~~
3. Which among the following is a point on the x axis ? 1  
 [(2, 0); (0, 2); (1, 1); (3, 4)]
4. Measure of the smallest angle of a right angled triangle is  $30^\circ$ . Length of its smallest side is 6 centimetres. What is the length of its largest side ? 1  
 (6, 3, 18, 12)





5. What is the slope of the line passing through the points (2, 5) and (3, 7)?

Score

1

(2, 3, 4, 5)

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{7-5}{3-2} = \frac{2}{1} = 2$$

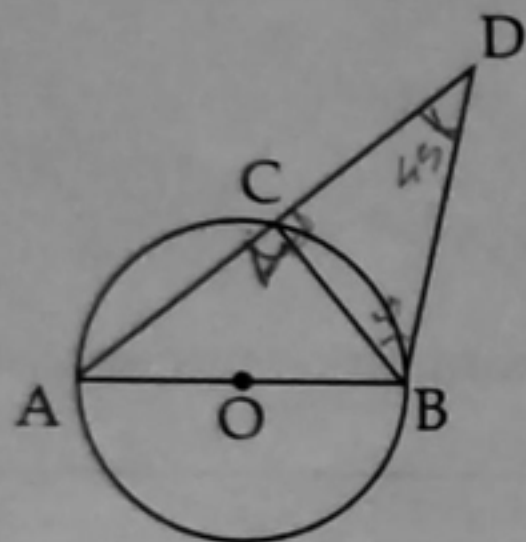
Questions from 6 to 10 carries 2 scores each.

5x2=10

6. Write the first term and common difference of the arithmetic sequence  $3n + 2$ .

2

7. In the figure AB is the diameter of the circle. C is a point on the circle. One of the angles  $\angle ACB$  and  $\angle ADB$  is twice the other.



Write the measures of the angles  $\angle ACB$  and  $\angle ADB$ .

8. One is asked to say a natural number less than 10.

1, 2, 3, 4, 5, 6, 7, 8, 9, 10

(a) What is the probability of it being an odd number?

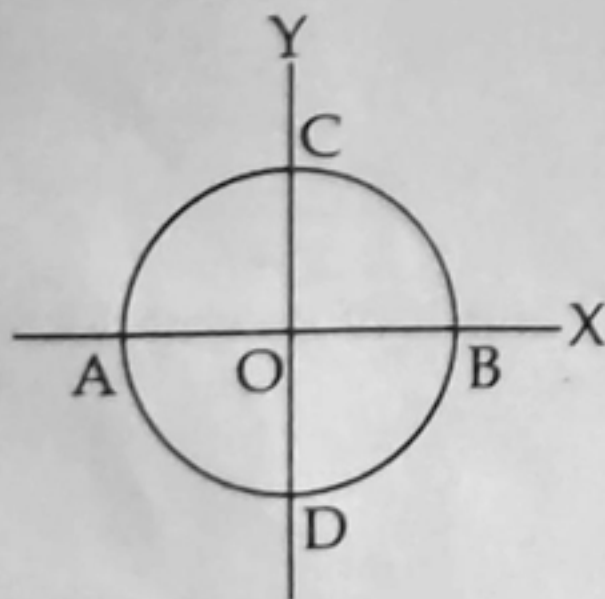
1

(b) What is the probability that it will not be an even number?

1

9.

2



In the figure, AB and CD are diameters of the circle. Coordinates of B are (3, 0). Write the coordinates of O and C.

10. Write  $x^2 - 1$  as the product of two first degree polynomials.

2



Questions from 11 to 20 carries 3 scores each.

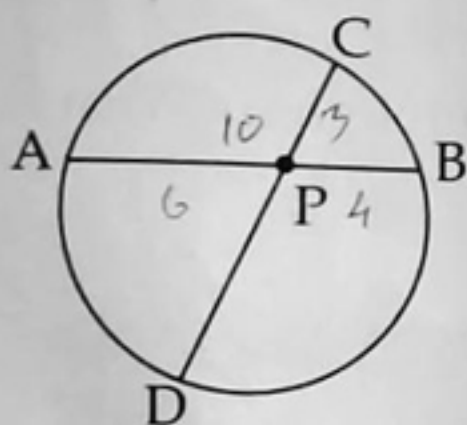
Score  
10x3=30

11. (a) What is the tenth term of the arithmetic sequence  $a + 1, a + 2, a + 3, \dots$ ? 1  
 (b) What is its common difference? 1  
 (c) Write the algebraic form of the above sequence. 1

12. Draw a triangle of circumradius 3 centimetres and two of the angles  $40^\circ$  and  $50^\circ$ . 3

13. (a) Write the sequence of even numbers. 1  
 (b) One added to the product of two consecutive even numbers gives 289. Form a second degree equation to solve this problem. 2

14. In the figure chords AB and CD intersect at P.  $AB = 10$  centimetres,  $PB = 4$  centimetres and  $PC = 3$  centimetres.

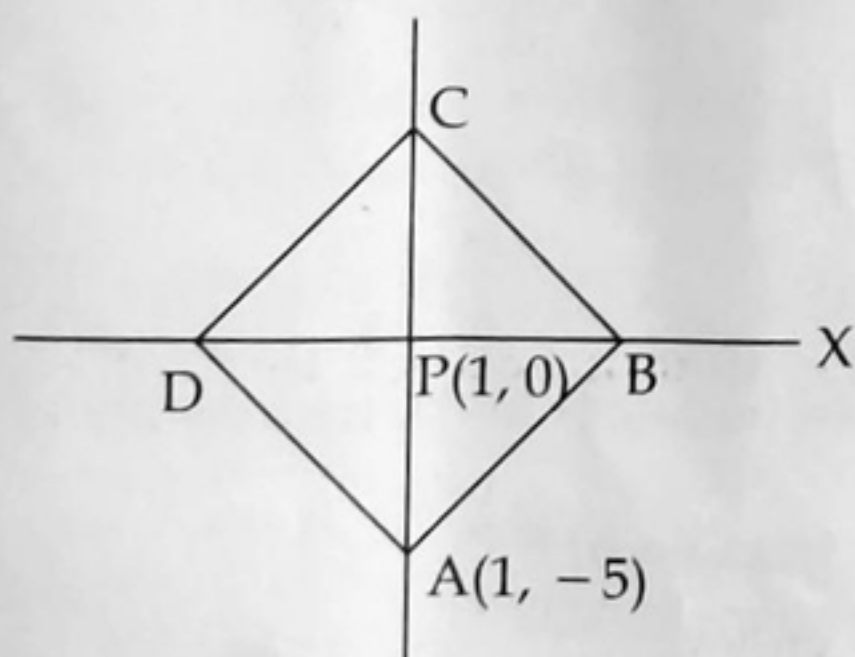


- (a) What is the length of PA? 1  
 (b) Find the length of PD. 2

15. P is at a distance of 13 centimetres from the centre of a circle of radius 5 centimetres.

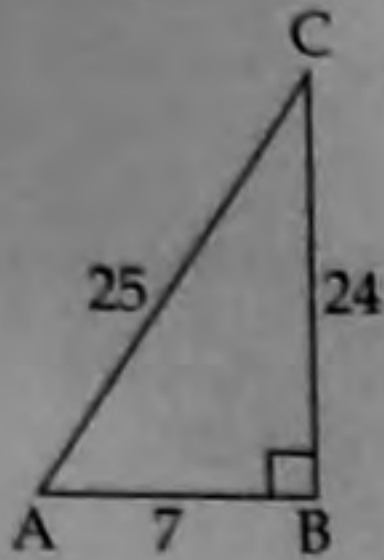
- (a) How many tangents can be drawn from the point P to the circle? 1  
 (b) Find the lengths of the tangents. 2

16. ABCD is a square, coordinates of A are  $(1, -5)$ . Diagonals of the square intersect at  $P(1, 0)$ . Write the coordinates of B, C and D. 3





17. In the figure  $\angle B = 90^\circ$ ,  $AB = 7$  centimetres,  $BC = 24$  centimetres,  $AC = 25$  centimetres.

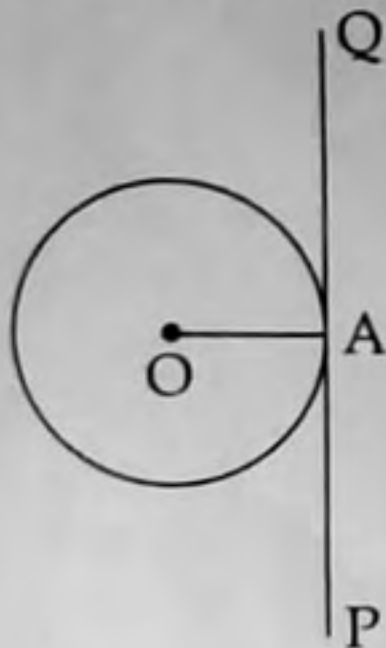


- (a)  $\sin A = \frac{24}{K}$ , what number is K? 1  
 (b) Write  $\cos C$  and  $\sin C$ . 2

18. A Sector of central angle  $120^\circ$  and radius 12 centimetres is rolled up into a cone.

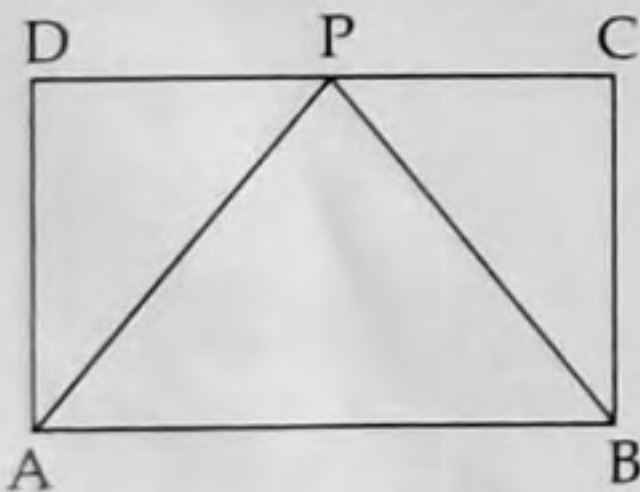
- (a) What is the slant height of the cone? 1  
 (b) Find the radius of the cone. 2

19. (a) In the figure  $OA$  is the radius of the circle.  $PQ$  is the tangent through  $A$ . What is the measure of  $\angle OAP$ ? 1



- (b) Draw a circle of radius 3 centimetres and mark a point A on it. Draw the tangent through A. 2

20.



ABCD is a rectangle. P is the mid-point of CD. If we put a dot in the figure without looking into it:

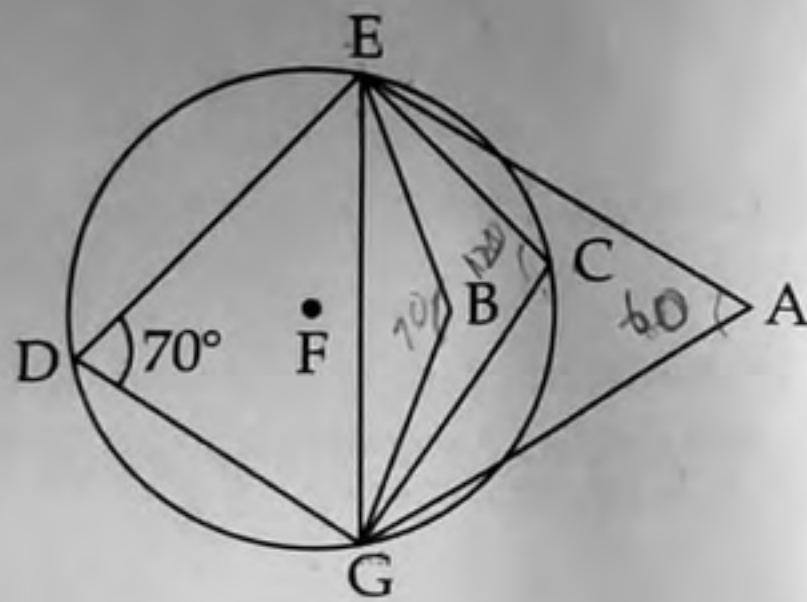
- (a) What is the probability that it would be inside triangle APB? 1  
 (b) What is the probability that it would be inside triangle ADP? 2

Questions from 21 to 30 carries 4 scores each.

Score  
10×4=40

21. (a) Write the 20<sup>th</sup> term of the arithmetic sequence 5, 10, 15, ..... 1  
(b) Find the sum of the first 20 terms of the arithmetic sequence 5, 10, 15, ..... 2  
(c) What is the sum of the first 20 terms of the arithmetic sequence 4, 9, 14, ..... ? 1

22.



In the figure C, D, E and G are points on the circle.  $\angle D = 70^\circ$ . For the angles given in column I choose suitable measures from column II.

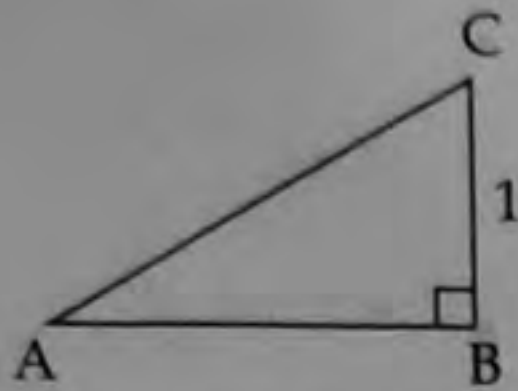
Column I	Column II
① $\angle ECG$	120° ②
② $\angle EBG$	60° ③
③ $\angle EAG$	110° ①
	180°

23. Fill up the empty cells of the given square such that the numbers in each row, each column and both diagonals form arithmetic sequences. 4

3	5	13
5	10	15
7	16	30



24. In the figure  $\angle B = 90^\circ$ .  $BC = 1$  centimetre,  $\sin A = \frac{1}{2}$ .



- (a) What is the length of AC ?  
 (b) Find the length of AB.  
 (c) What is the measure of  $\angle A$  ?  
 (d)  $\sin 60^\circ =$  \_\_\_\_\_.

1  
1  
1  
1

25. Draw a circle of radius 3 centimetres. Mark a point P outside the circle at a distance 7 centimetres from the centre. Draw tangents from P to the circle. Measure the length of the tangents. 4

26. Scores of 10 students are given below :

11, 32, 33, 35, 39, 41, 45, 47, 48, 49

- (a) Find the mean score.  
 (b) Find the median score.

2  
2

27. Draw the  $x$  and  $y$  axes. Mark the point  $(2, 3)$ . Draw a circle with origin as centre and passing through the point  $(2, 3)$ . 4

28. (a) The perimeter of a rectangle is 40 centimetres. Length of its smaller side is 7 centimetres. What is the length of its larger side ? 1  
 (b) Find the sides of a rectangle with perimeter 40 centimetres and area 96 square centimetres. 3

29. One is asked to say a two-digit number,

- (a) What is the probability of both digits being the same ?  
 (b) What is the probability of the first digit being twice the second ?

2  
2

30. (a)  $P(x) = x^2 - 5x + 9$ , find  $P(2)$  and  $P(3)$ .

2

- (b) Write  $P(x) - P(2)$  as the product of two first degree polynomials.

2



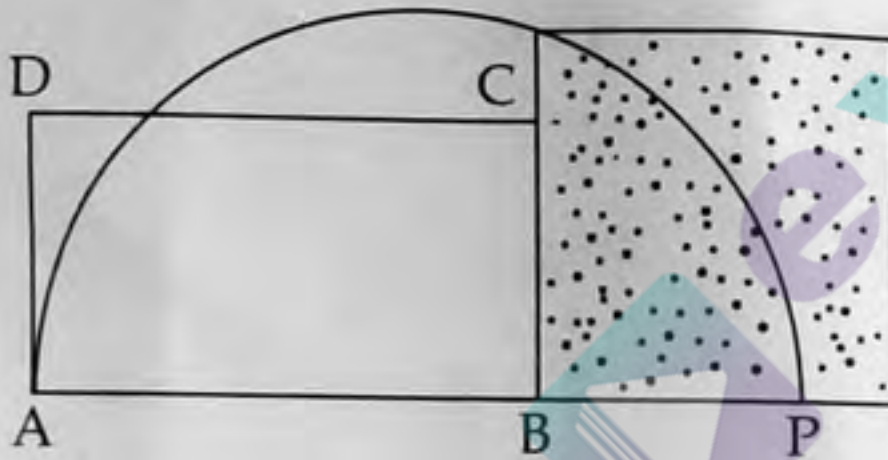
Questions from 31 to 45 carries 5 scores each.

Score  
15x5=75

31. 1  
2 3  
4 5 6  
7 8 9 10  
.....

- (a) Write the fifth line of the pattern. 1  
(b) How many numbers are there in the tenth line? 1  
(c) How many numbers are there in the first ten lines altogether? 2  
(d) What is the first number in the eleventh line? 1

32. (a) In the figure area of the rectangle ABCD is 8 square centimetres and  $BC = BP$ . 1



What is the area of the shaded square?

- (b) Draw a rectangle of area 8 square centimetres. Draw a square having the same area of the rectangle. 4

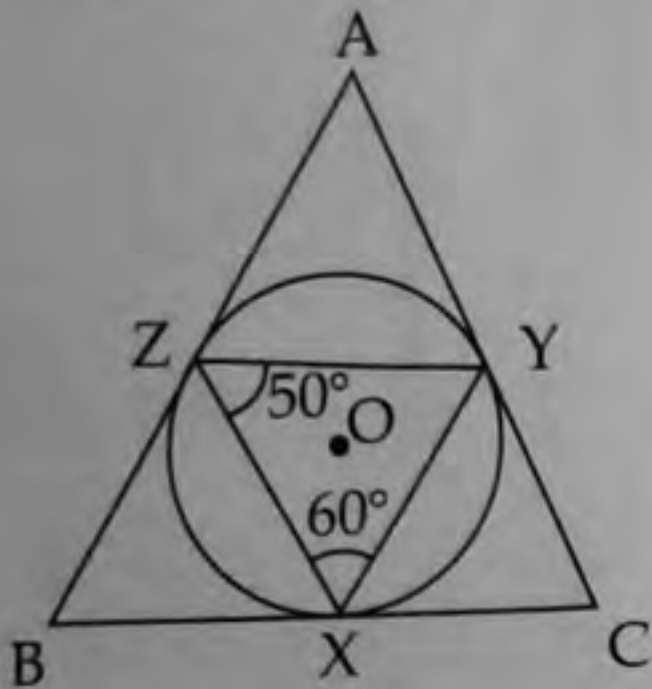
33. A man standing at the edge of a river sees the top of a tree at an elevation of  $60^\circ$ . Stepping 20 metres back he sees it at an elevation of  $30^\circ$ . Draw a rough figure and find the width of the river. 5

34. The sides of a rectangle are parallel to the axes. One pair of its opposite vertices are  $A(2, 4)$  and  $C(6, 12)$ .

- (a) Write the coordinates of the other two vertices. 2  
(b) Write the coordinates of the mid-point of AC. 2  
(c) x coordinate of a point on AC is 'a'. What is its y coordinate? 1

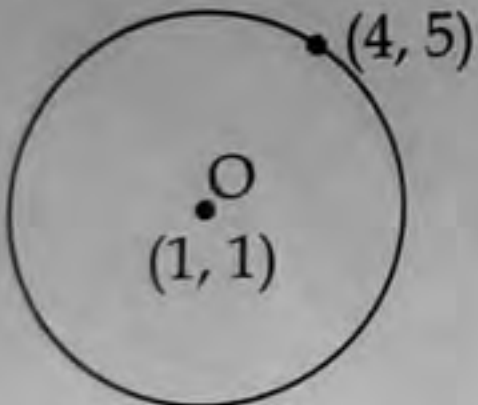


35. In the figure AB, BC and AC touches the circle at the points Z, X and Y.  $\angle ZXY = 60^\circ$  and  $\angle XZY = 50^\circ$ . Find the measures of  $\angle A$ ,  $\angle B$  and  $\angle C$ . 5



36. (a) Radius of a solid metal cone is 5 centimetres, its slant height is 13 centimetres. Find its height. 2  
 (b) Find the volume of the cone. 1  
 (c) It is melted and recast into small cones of radius 1 centimetre and height one centimetre. How many cones will we get? 2

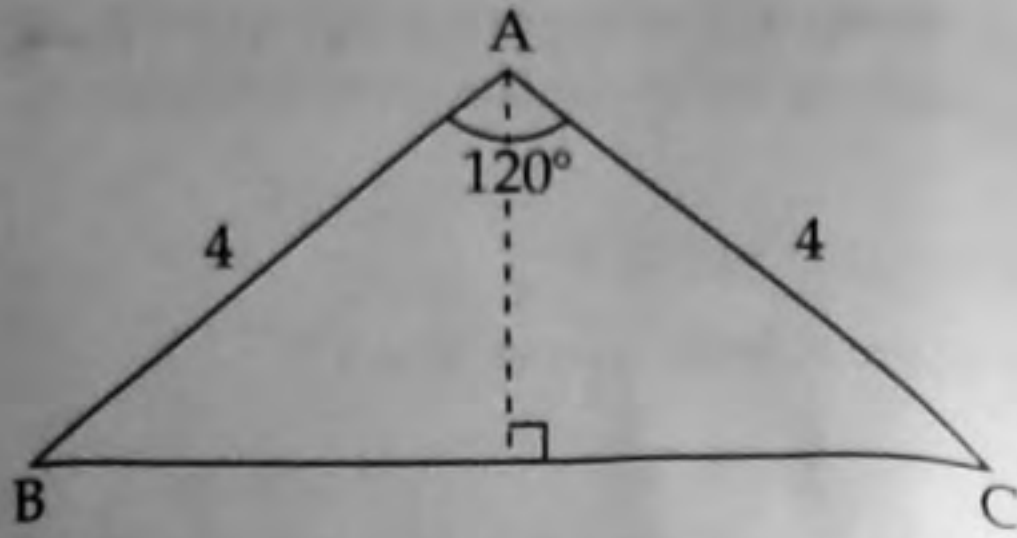
37. A circle is drawn with (1, 1) as centre. (4, 5) is a point on the circle.



- (a) Find the radius of the circle. 1  
 (b) Write the equation of the circle. 2  
 (c) The x coordinate of a point on the circle is 6. What is the y coordinate of that point? 2
38. The diameters of two spheres are in the ratio 1 : 2. 1  
 (a) What is the ratio of their radii? 3  
 (b) Find the ratio of their surface areas. 1  
 (c) If the surface area of the first sphere is  $10\pi$  square centimetres. What is the surface area of the second sphere?
39. (a) What is the remainder on dividing the terms of the arithmetic sequence 100, 109, 118, ..... by 9? 1  
 (b) Write the sequence of three digit numbers, which are multiples of 9. 2  
 (c) What is the position of 999 in the arithmetic sequence of three digit numbers which are multiples of 9? 2



40.



In the figure  $AB = AC = 4$  centimetres,  $\angle A = 120^\circ$ .

- (a)  $\angle B = \underline{\hspace{2cm}}$ .  
 (b) Find the perpendicular distance from A to BC.  
 (c) Find the area of the triangle.

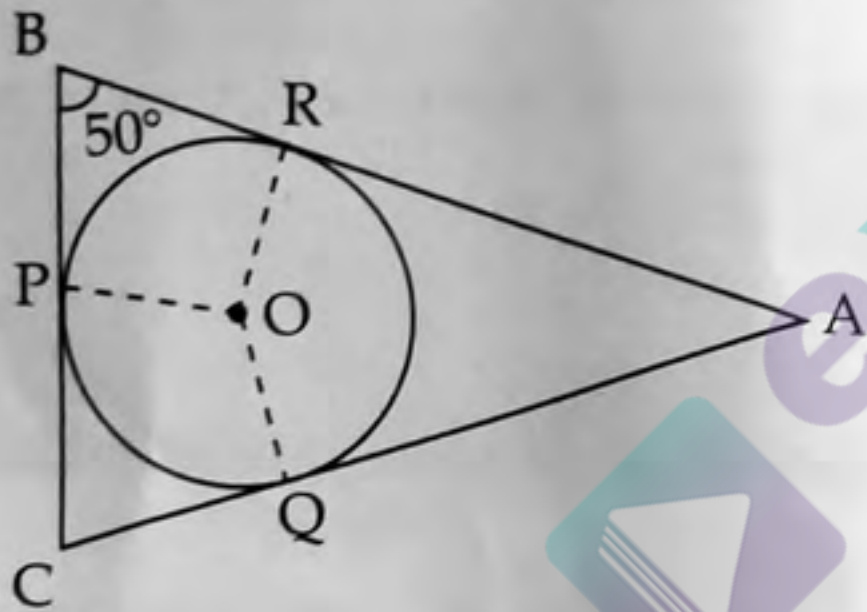
1

2

2

41.

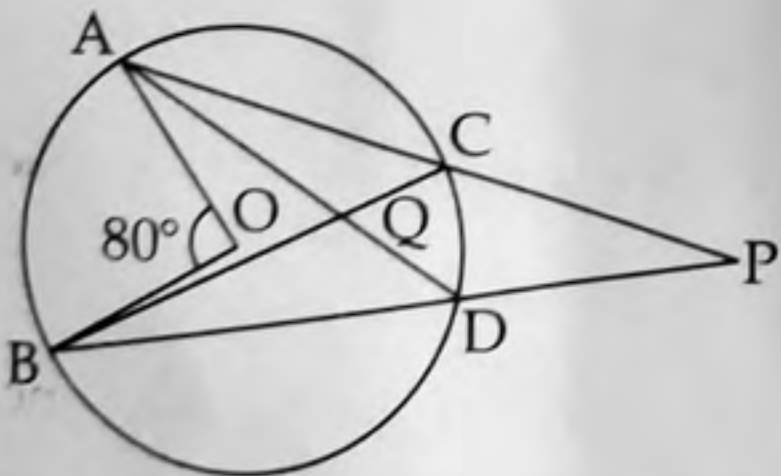
- (a) In the figure, circle with centre O touches the sides of the triangle ABC at the points P, Q and R. If  $\angle B = 50^\circ$ , what is  $\angle POR$ ? 1



- (b) Draw a circle of radius 2.5 centimetres. Draw a triangle of angles  $50^\circ, 60^\circ, 70^\circ$  with all its sides touching the circle. 4

42.

- In the figure, O is the centre of the circle. A, B, C and D are points on the circle.  $\angle AOB = 80^\circ$ .



- (a) Write the measures of  $\angle ACB$ ,  $\angle ADB$  and  $\angle ADP$ .  
 (b) Find  $\angle CQD + \angle P$ .

3

2



43. A box is to be made by cutting off small squares from each corner of a square of thick paper, and bending upwards. The height of the box is to be 10 centimetres and volume 1 litre.
- (a) What should be the length of a side of the square cut-off? 1
- (b) What should be the length of a side of the square, thick paper sheet? 4

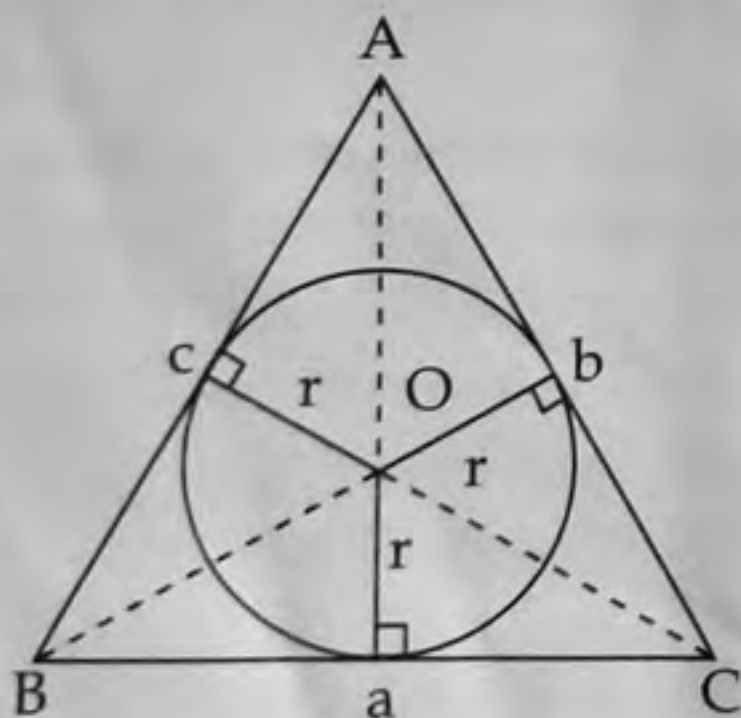
44. The table below shows, children of a class sorted according to their scores in an examination.

Scores	Number of Children
0 - 10	5
10 - 20	8
20 - 30	10
30 - 40	13
40 - 50	9
Total	45

- (a) If the children are arranged in the ascending order of their scores, then what will be the assumed score of the 14<sup>th</sup> child? 1
- (b) Compute the median score. 4

45. Read the following passage. Understand the mathematical concept in it and answer the questions that follow.

Circle passing through all the three vertices of a triangle is its circumcircle. Like this, the circle touching all the three sides of a triangle is its incircle. The point of intersection of the angle bisectors is the incentre.



Distance from the centre of the circle to the touching point is radius.

Area of triangle ABC is the sum of the areas of the triangles OBC, OAC and OAB. If the radius of the incircle is taken as  $r$  and the sides of the triangle as  $a$ ,  $b$  and  $c$ .



$$\begin{aligned}
 \text{Then area of triangle } ABC &= \frac{1}{2}ar + \frac{1}{2}br + \frac{1}{2}cr \\
 &= \frac{1}{2}r(a + b + c) \\
 &= r \frac{(a + b + c)}{2} \\
 &= r \times s
 \end{aligned}$$

Here  $s = \frac{a + b + c}{2}$  (half of perimeter)

- (a) Circle touching all the three sides of a triangle is : 1  
[circumcircle, incircle, semicircle, ellipse]
- (b) Circle passing through all the three vertices of a triangle is : 1  
[circumcircle, incircle, semicircle, ellipse]
- (c) If the radius of the incircle is taken as  $r$  and the half of the perimeter as  $s$  then area of the triangle is : 1  
 $\left( r + s, \frac{r}{s}, r \times s, r^2 \times s \right)$
- (d) The perimeter of a triangle is 20 centimetres and radius of its incircle is 2 centimetres. What is the area of the triangle ? (in square centimetres) 1  
(40, 20, 10, 5)
- (e) Area of a triangle is 24 square centimetres and its perimeter is 24 centimetres. Radius of the incircle is \_\_\_\_\_ centimetres. 1  
(1, 2, 1.5, 2.5)

